

(I) Complete the following:-

Name : Class :

- 1) $12 : \dots = 4 : 5$
- 2) $x^2 : y = 4x^2y : \dots$
- 3) $\frac{a^2c}{b^2d} : \frac{ac^2}{d^2b} = \dots : bc$
- 4) The proportion is
- 5) If $\frac{a}{b} = \frac{5}{7}$ then $a = \dots, b = \dots$
- 6) If $\frac{x}{y} = \frac{Z}{L} = \frac{5}{4}$, then $\frac{x+z}{y+l} = \dots$
- 7) If $\frac{a}{2} = \frac{b}{3} = \frac{5a-2b}{c}$, then $c = \dots$
- 8) If a, b, c are proportional , then $b = \dots$
- 9) If $\frac{y}{x} = \frac{x}{z} = \frac{2}{5}$ then $y = \dots z$
- 10) The real numbers which make $(x+1), (x+5), (x+13)$ are proportional is
- 11) If $x, \sqrt{8}, 7, 14\sqrt{2}$ are four proportional quantities, then $x = \dots$
- 12) If $x : y = 3 : 1, x + y = 28$, then $x = \dots, y = \dots$
- 13) If $\frac{a}{b} = \frac{3}{5}, \frac{a}{c} = \frac{3}{7}$, then $\frac{c}{b} = \dots$
- 14) If $x \propto y$ then $x = \dots$
- 15) If $y \propto x^2$, then $y = \dots$
- 16) If y varies inversely as x then y varies directly as
- 17) If $y \propto x^2$ when z is constant of $y \propto \frac{1}{z}$ when x is constant , then $y \propto \dots$
- 18) If $a \propto \frac{1}{b}$, then $\frac{a_1}{a_2} = \dots$
- 19) The point of intersection of the two straight lines $y = -1, x - 2y = 1$ is
- 20) If $\frac{a+b}{a+2b} = \frac{2}{5}$ then $a : b = \dots$

21) If 10 is the middle proportion between 4 , x then x =

22) If $\frac{a}{b} = \frac{b}{c} = \frac{c}{3} = 2$ then a =

23) If 4 , -10 , 5 x are proportional , then x =

24) If $2xy = 3$ then ($y \propto x$, $y \propto \frac{1}{x}$, $y = \frac{1}{x}$, $y = \frac{2}{3}x$)

25) If y varies inversely as (x + 4) , if y = 4 as x = 1 then the constant of the variation is

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(2)a) :-

If $\frac{x}{y} = \frac{2}{3}$, then find $\frac{x^2 + 2xy - y^2}{6xy}$

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b) Find the positive number which if we subtracted it's square from each of the two terms

of the ratio $\frac{41}{91}$ the rest will be $\frac{1}{3}$

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.....

(3)a) :- $x^2 + 64y^2 = 16xy$, then find $\frac{2x+3y}{x-5y}$

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.....

b) If $\frac{a}{2x+y} = \frac{b}{3y-x} = \frac{c}{4x+5y}$ then prove that $\frac{a+2b}{4b+c} = \frac{7}{17}$

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(4) :- If $y \propto (x-1)$, $y \propto \frac{1}{x}$ then find the relation between x & y if x = 3 and y = 2

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(5):- If $2a = 3b = 4c$, then find $a : b : c$

(6):- If $x \times y = \{ (1,1), (1,3), (1,5) \}$ find:

- a) x, y b) $y \times x$ c) y^2

(6):- If $x = \{ 3,4 \}$, $y = \{ 4,5 \}$ and $z = \{ 6,5 \}$, find:

- a) $x \times (y \cap z)$ b) $(x-y) \times z$ c) $(x-y) \times (y-z)$

(8):- Graph the linear fraction $f(x) = 3x - 1$ then find the point of intersection of the straight line with the two axes.

(9):- Represent graphically the function $f: f(x) = x^2 - 2$ taken $x \in [-3,3]$ and from the graph deduce the coordinates of point of vertex of curve, the equation of the axis of symmetry and the minimum or maximum value of the function .

Name : Class :

(1) Complete the following:-

1) $12 : \dots \cdot 5 \dots = 4 : 5$

2) $x^2 : y = 4x^2y : \dots 4 \cdot y^2 \dots$

3) $\frac{a^2c}{b^2d} : \frac{ac^2}{d^2b} = \dots a \cdot d \dots : bc$

4) The proportion is ...the equality of two or more ratios

5) If $\frac{a}{b} = \frac{5}{7}$ then $a = \dots 5m \dots$, $b = \dots 7m \dots$

6) If $\frac{x}{y} = \frac{z}{l} = \frac{5}{4}$, then $\frac{x+z}{y+l} = \dots \frac{5}{4} \dots$

7) If $\frac{a}{2} = \frac{b}{3} = \frac{5a-2b}{c}$, then $c = \dots 14 \dots$

8) If a, b, c are proportional, then $b = \dots \pm \sqrt{ac} \dots$

9) If $\frac{y}{x} = \frac{x}{z} = \frac{2}{5}$ then $y = \dots \frac{4}{25} \dots z$

10) The real numbers which make $(x+1), (x+5), (x+13)$ are proportional is ... 3 ...

11) If $x, \sqrt{8}, 7, 14\sqrt{2}$ are four proportional quantities, then $x = \dots 1 \dots$

12) If $x : y = 3 : 1$, $x + y = 28$, then $x = \dots 21 \dots$, $y = \dots 7 \dots$

13) If $\frac{a}{b} = \frac{3}{5}, \frac{a}{c} = \frac{3}{7}$, then $\frac{c}{b} = \dots \frac{7}{5} \dots$

14) If $x \propto y$ then $x = \dots m \cdot y \dots$

15) If $y \propto x^2$, then $y = \dots m \cdot x^2 \dots$

16) If y varies inversely as x then y varies directly as .. $\frac{1}{x} \dots$

17) If $y \propto x^2$ when z is constant of $y \propto \frac{1}{z}$ when x is constant, then $y \propto \dots \frac{x^2}{z} \dots$

18) If $a \propto \frac{1}{b}$, then $\frac{a_1}{a_2} = \dots \frac{1}{2} \dots$

19) The point of intersection of the two straight lines $y = -1$, $x - 2y = 1$ is ... (-1, -1) ...

20) If $\frac{a+b}{a+2b} = \frac{2}{5}$ then $a : b = \dots 1 : 3 \dots$

21) If 10 is the middle proportion between 4 , x then $x = \dots 2.5 \dots$

22) If $\frac{a}{b} = \frac{b}{c} = \frac{c}{3} = 2$ then $a = \dots 24 \dots$

23) If 4 , -10 , 5 x are proportional , then $x = \dots 5 \dots$

24) If $2xy = 3$ then $\dots y \propto \frac{1}{x} \dots$ ($y \propto x$, $y \propto \frac{1}{x}$, $y = \frac{1}{x}$, $y = \frac{2}{3}x$)

25) If y varies inversely as $(x + 4)$, if $y = 4$ as $x = 1$ then the constant of the variation is $\dots 25 \dots$

(2a) :-

If $\frac{x}{y} = \frac{2}{3}$, then find $\frac{x^2 + 2xy - y^2}{6xy}$ $x = 2m$, $y = 3m$

$$\frac{(2m)^2 + 1(2m)(3m) - (3m)^2}{6(2m)(3m)} = \frac{4m^2 + 12m^2 - 9m^2}{36m^2} = \frac{7m^2}{36m^2} = \frac{7}{36}$$

b) Find the positive number which if we subtracted it's square from each of the two terms

of the ratio $\frac{41}{91}$ the rest will be $\frac{1}{3}$

$$\frac{41 - x^2}{91 - x^2} = \frac{1}{3} \quad \therefore 91 - x^2 = 123 - 3x^2 \quad \therefore 3x^2 - x^2 = 123 - 91 \\ \therefore 2x^2 = 32 \quad \therefore x^2 = 16 \quad \therefore x = \sqrt{16} = 4$$

(-4) infreal.

(3a) :- $x^2 + 64y^2 = 16xy$, then find $\frac{2x+3y}{x-5y}$

$$... x^2 + 64y^2 = 16xy \quad \therefore x = 8y \quad \therefore \frac{2x+3y}{x-5y} = \frac{2(8y)+3y}{8y-5y} = \frac{19y}{3y} = \frac{19}{3}$$

$$(x+2y)(x-2y)=0 \quad \therefore \frac{2}{y} = \frac{8}{1} \quad \therefore y = m \quad = \frac{19m}{3m} = \frac{19}{3}$$

b) If $\frac{a}{2x+y} = \frac{b}{3y-x} = \frac{c}{4x+5y}$ then prove that $\frac{a+2b}{4b+c} = \frac{7}{17}$

$$\frac{a+2b}{2x+y} = \frac{a+2b}{3y-x} \quad \left| \begin{array}{l} 4b+c \\ 12y-4x+4x+5y \end{array} \right. = \frac{4b+c}{17y} \quad \therefore \frac{a+2b}{4b+c} = \frac{7y}{17y} = \frac{7}{17}$$

(4) :- If $y \propto (x-1)$, $y \propto \frac{1}{x}$ then find the relation between x & y if $x = 3$ and $y = 2$

$$y \propto \frac{x-1}{x} \quad \therefore y = m \left(\frac{x-1}{x} \right) \quad \therefore y = m \left(1 - \frac{1}{x} \right) \quad \left| \begin{array}{l} y = \frac{y}{m} \left(1 - \frac{1}{x} \right) \\ = 2 \div \left(1 - \frac{1}{3} \right) \end{array} \right. \\ = 2 \div \left(1 - \frac{1}{3} \right) = 3$$

$$\textcircled{2} \quad \therefore y = 3 \left(1 - \frac{1}{x} \right)$$

(5):- If $2a = 3b = 4c$, then find $a : b : c$

$$\frac{2a}{12} = \frac{3b}{12} = \frac{4c}{12} \therefore \frac{a}{6} = \frac{b}{4} = \frac{c}{3} \text{ so, } a:b:c = 6:4:3$$

(6):- If $x \times y = \{(1,1), (1,3), (1,5)\}$ find:

- a) $x \cdot y$ b) $y \times x$ c) y^2

$$x = \{1\}, y = \{1, 3, 5\}$$

$$y \times x = \{(1,1), (3,1), (5,1)\}$$

$$y^2 = \{(1,1), (1,3), (1,5), (3,1), (3,3), (3,5), (5,1), (5,3), (5,5)\}$$

(6):- If $x = \{3,4\}$, $y = \{4,5\}$ and $z = \{6,5\}$, find:

- a) $x \times (y \cap z)$ b) $(x-y) \times z$ c) $(x-y) \times (y-z)$

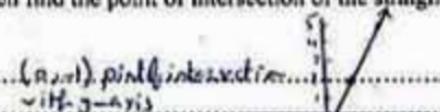
$$x = \{3,4\}, y \cap z = \{4\}, z = \{5\} \therefore \{3,4\} \times \{5\} = \{(3,5), (4,5)\}$$

$$(x-y) \times z = \{3\} \times \{5\} = \{(15)\}$$

$$(x-y) \times (y-z) = \{3\} \times \{4\} = \{(12)\}$$

(8):- Graph the linear fraction $f(x) = 3x - 1$ then find the point of intersection of the straight line with the two axes.

$$\text{Point on } y \text{ axis: } f(x) = 3(0) - 1 = -1 \quad (0, -1) \text{ point of intersection with } y \text{ axis}$$



$$\text{Point on } x \text{ axis: } f(x) = 0 \therefore 3x - 1 = 0 \therefore x = \frac{1}{3} \quad (\frac{1}{3}, 0) \text{ point of intersection with } x \text{ axis}$$

(9):- Represent graphically the function $f: f(x) = x^2 - 2$ taken $x \in [-3, 3]$ and from the graph deduce the coordinates of point of vertex of curve, the equation of the axis of symmetry and the minimum or maximum value of the function.

$$\text{Point of vertex of curve: } (0, -2)$$

$$\text{Eq. of axis of symmetry: } x = 0$$

$$\text{min. value} = -2$$

